

## Change of Concentration in a Tank

("continuously-stirred tank reactor")

$V$  = volume of the tank

$q$  = flow rate through the tank (= inlet flow rate, and = outlet flow rate)

$t$  = time;  $t = 0$  is the "initial" time

$f, t$  = tank concentration at time  $t$ ;  $f, 0$  = initial tank concentration

$w$  = inlet concentration

task: solve for  $f$  in terms of  $V$ ,  $q$ ,  $f, 0$ ,  $w$ , and any other known functions

Solution:

rate of change of concentration  
at time  $t = f', t$

$$= \left( \frac{\text{mass in} - \text{mass out}}{\text{volume}} \right)$$

$$= \frac{qw - qf, t}{V}$$

$$\therefore f' = \frac{qw - qf}{V}$$

$$\therefore \frac{f'}{f-w} = \frac{-q}{V}$$

$$\therefore \int \frac{f'}{f-w} = \int \frac{-q}{V} + C_1$$

$$\therefore \lambda \cdot (f-w) + C_2 = \left( \frac{-q}{V} + C_3 \right) + C_1$$

$$\therefore \lambda \cdot (f-w) = \frac{-q}{V} + C_4$$

$$\therefore f-w = \epsilon \cdot \left( \frac{-q}{V} + C_4 \right)$$

$$\therefore f-w = (\epsilon \cdot C_4) \epsilon \cdot \left( \frac{-q}{V} \right)$$

$$\therefore f-w = c \epsilon \cdot \left( \frac{-q}{V} \right)$$

$$\therefore f = w + c \epsilon \cdot \left( \frac{-q}{V} \right)$$

$$\therefore f, 0 = w + c$$

$$\therefore c = f, 0 - w$$

$$\therefore f = w + (f, 0 - w) \epsilon \cdot \left( \frac{-q}{V} \right)$$

DONE