

## The number of items in a summation

In the summation

$$\sum_{k=a}^b \dots ,$$

$b$  does not tell the number of items, but is merely the upper limit on the value of  $k$ .  
The number of items in the summation is

$$b - a + 1.$$

(When  $a = 1$ , then  $b$  coincides with the number of items, but that is merely a coincidence.)

Consider the example

$$\sum_{k=-2}^3 (8-k) .$$

This has  $3 - (-2) + 1 = 6$  items, and the summation of these 6 items is:

$$(8 - (-2)) + (8 - (-1)) + (8 - 0) + (8 - 1) + (8 - 2) + (8 - 3)$$

$$= 10 + 9 + 8 + 7 + 6 + 5 = 45.$$

(end of document)